Measurements of the instantaneous velocity difference and the local velocity with a fiber-optic coupler

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New optical arrangements with two single-mode input fibers and a fiber-optic coupler are devised to measure the instantaneous velocity difference and the local velocity. The fibers and the coupler are polarization-preserving to guarantee a high signal-to-noise ratio. When the two input fibers are used to collect the scattered light with the same momentum-transfer vector but from two spatially separated regions in a flow, the obtained signals interfere when combined via the fiber-optic coupler. The resultant light received by a photomultiplier tube contains a cross-beat frequency proportional to the velocity difference between the two measuring points. If the two input fibers are used to collect the scattered light from a common scattering region but with two different momentum-transfer vectors, then the resultant light contains a self-beat frequency proportional to the local velocity at the measuring point. The experiment shows that both the cross-beat and the self-beat signals are large and that the standard laser Doppler signal processor can be used to measure the velocity difference and the local velocity in real time. The new technique will have various applications in the general area of fluid dynamics. © 2001 Optical Society of America

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1. INTRODUCTION

Measurements of the velocity difference or the relative velocity, \( \delta v(l) = v(x + l) - v(x) \), between two spatial points separated by a distance \( l \) have important applications in fluid dynamics. For example, in the study of turbulent flows one is interested in the scaling behavior of \( \delta v(l) \) over varying distance \( l \) when \( l \) is in the inertial range, in which the kinetic energy cascades at a constant rate without dissipation.\(^1\) If the separation \( l \) is smaller than the Kolmogorov dissipation length,\(^1\) the measured \( \delta v(l) \) becomes proportional to the velocity gradient \( \partial v / \partial l = \delta v(l)/l \) (assuming \( l \) is known), a useful quantity that is needed to determine the energy dissipation and the flow vorticity. In many experimental studies of fluid turbulence, one measures the local velocity as a function of time and then uses Taylor’s frozen-turbulence assumption to convert the measured temporal variations into the spatial fluctuations of the velocity field.\(^3\) The frozen-turbulence assumption is valid only when the mean velocity becomes much larger than the velocity fluctuations. For isotropic turbulent flows with a small mean velocity, direct measurement of \( \delta v(l) \) is needed.

Over the past several years, the present authors and their collaborators have exploited the technique of homodyne photon correlation spectroscopy (HPCS) to measure \( \delta v(l) \).\(^4\) In the HPCS scheme, small particles seeded in a flowing fluid are used to scatter the incident laser light. The scattered light intensity \( I(t) \), which fluctuates because of the motion of the seed particles, contains Doppler beat frequencies of all particle pairs in the scattering volume. For each particle pair separated by a distance \( l \) (along the beam-propagation direction), their beat frequency is \( \Delta \omega = q \cdot \delta v(l) \), where \( q \) is the momentum-transfer vector. The magnitude of \( q \) is given by \( q = (4\pi n/\lambda)\sin(\theta/2) \), where \( \theta \) is the scattering angle, \( n \) is the refractive index of the fluid, and \( \lambda \) is the wavelength of the incident light. Experimentally, the Doppler beat frequency \( \Delta \omega \) is measured by the intensity autocorrelation function.\(^6\)

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states that the light scattered by each pair of particles with separation \( r \) values spanned by the detecting area. In the experiment,\(^5\) two single-mode, polarization-maintaining fibers are used to collect light with the same polarization and momentum-transfer vector \( \mathbf{q} \) but from two spatially separated regions in a flow. These regions are illuminated by a single coherent laser beam so that the collected signals interfere when combined by using a fiber-optic coupler, before being directed to a photodetector. With this arrangement, the measured \( G(\tau) \) becomes proportional to the Fourier cosine transform of the PDF \( P(\delta \mathbf{v}, r) \).

The second limitation of HPCS is related to signal processing. The correlation method is very effective in picking up small fluctuating signals, but the resulting correlation function \( G(\tau) \) is a time-averaged quantity. Therefore the correlation method is not applicable to unstable flows. Furthermore, information about the odd moments of \( P(\delta \mathbf{v}, r) \) is lost, because the measured \( G(\tau) \) is a Fourier cosine transform of \( P(\delta \mathbf{v}, r) \).

In this paper we present a further improvement for HPCS that is free of the two limitations discussed above. By combining the new fiber-optic method with laser Doppler velocimetry (LDV) electronics, we are able to measure the instantaneous velocity difference \( \delta \mathbf{v}(l, t) \) and local velocity \( \mathbf{v}(x, t) \) at a high sampling rate. With this technique, the statistics of \( \delta \mathbf{v}(l, t) \) and \( \mathbf{v}(x, t) \) are obtained directly from the time-series data. The new method of measuring \( \mathbf{v}(x, t) \) offers several advantages over the standard LDV. The remainder of the paper is organized as follows: In Section 2 we describe the experimental methods and setup. Experimental results are presented and analyzed in Section 3. Finally, the work is summarized in Section 4.

![Fig. 1](image-url) (a) Scattering geometry for the velocity difference measurement. \( \mathbf{q} \), incident wave vector; \( \mathbf{k}_s \), scattered wave vector; \( \mathbf{q} = \mathbf{k}_s - \mathbf{k}_l \). (b) Experimental setup for the velocity difference measurement in rigid body rotation. (c) Flow cell and optical arrangement for a jet flow.
2. EXPERIMENTAL METHODS

A. Measurement of the Velocity Difference

Figure 1 shows the optical arrangement and the flow cells used in the experiment. A similar setup has been described elsewhere, and here we mention only some key points. As shown in Fig. 1(b), an incident beam from a Nd:YVO4 laser with a power range of 0.5–2 W and a wavelength of \( \lambda = 532 \) nm is directed to a flow cell by a lens. With the aid of a large beam-splitting cube, two single-mode PM fibers collect the scattered light from two different spots along the laser beam with a separation \( L \). The two PM fibers are connected to a fiber-optic coupler (purchased from Oz Optics,11) which combines the light from the two input fibers and splits the resultant light evenly into two output fibers. A graded-index lens is placed at each end of the fiber to collimate the light entering (or exiting) the fiber core. Each input fiber is mounted on a micrometer-controlled translation stage, and the distance \( L \) can be adjusted in a range of 0–25 mm in steps of 0.01 mm. The output fibers of the optical coupler are connected to two photomultiplier tubes, PMT1 and PMT2. PMT1 is operated in the digital mode, and its output signal is fed to a digital correlator (ALV-5000). PMT2 is operated in the analog mode, and its output signal is fed to a LDV signal processor (TSI IFA655). An oscilloscope directly connected to PMT2 views the analog signals. A low-noise preamplifier (Stanford Research SR560) further amplifies the analog output of PMT2 before it goes to the LDV signal processor.

As shown in Fig. 1(a), the electric fields detected by each input fiber sum in the coupler and consequently interfere. In the experiment, we obtain the beat frequency, \( \Delta \omega _2 = q \cdot \mathbf{v}_1 - q \cdot \mathbf{v}_2 = q \cdot \Delta \mathbf{v}(L) \), in two different ways. One way is to measure the intensity autocorrelation function \( g(\tau) \) (in Eq. (1)). With the ALV correlator, it takes \( \sim 1 \) min to collect the data with an adequate signal-to-noise ratio. Another way is to use the LDV signal processor to measure the instantaneous beat frequency \( \Delta \omega _2 \), giving velocity differences in real time. The LDV signal processor is essentially a very fast correlator and thus requires the beat signal to be large enough that no signal averaging is needed. In the experiment to be discussed below, we use both methods to analyze the beat signals and compare the results.

It has been shown that the correlation function \( g(\tau) \) has the form

\[
g(\tau) = 1 + \frac{I_1^2 + I_2^2}{(I_1 + I_2)^2} G_s(\tau) + \frac{2I_1I_2}{(I_1 + I_2)^2} G_c(\tau)
\]

\[
= 1 + b_s G_s(\tau) + b_c G_c(\tau),
\]

where \( I_1 \) and \( I_2 \) are the light intensities from the two input fibers. When \( I_1 = I_2 \), one finds \( b_s = b_c = 0.5 \). If one of the input fibers is blocked (i.e., \( I_2 = 0 \)), we have \( g(\tau) = 1 + G_s(\tau) \), where \( G_s(\tau) \) is the self-beat correlation function for a single fiber. When the separation \( L \) between the two input fibers is much larger than the spot size viewed by each fiber, the cross-beat correlation function \( G_c(\tau) \) takes the form

\[
G_c(\tau) = G_s(\tau) \int_{-\infty}^{+\infty} d\delta v P(\delta v) \cos(q \delta v(L) \tau).
\]

Two flow cells are used in the experiment. The first one is a cylindrical cuvette having an inner diameter of 2.45 cm and a height of 5 cm. The cuvette is top mounted on a geared motor, which produces smooth rotation with an angular velocity \( \omega = 2.5 \) rad/s. The cell is filled with 1.2-propylene glycol, which is 40 times more viscous than water. The whole cell is immersed in a large, square index-matching vat, which is also filled with 1.2-propylene glycol. The flow field inside the cell is a simple rigid-body rotation. With the scattering geometry shown in Fig. 1(b), the beat frequency is given by \( \Delta \omega _2 = k \omega L \), with \( k_s = 2 \pi n/\lambda \). The sample cell is seeded with a small amount of polystyrene latex spheres. For the correlation measurements, we use small seed particles 1.0 \( \mu m \) in diameter. By using the small seed particles, one can have more particles in the scattering volume even at low seeding densities. This will reduce the amplitude of the number fluctuations caused by the change in the number of particles in each scattering volume. The particle-number fluctuations can produce incoherent amplitude fluctuations in the scattered light and thus introduce an extra (additive) decay to \( g(\tau) \). Large particles 4.75 \( \mu m \) in diameter are used to produce higher scattering intensity for instantaneous Doppler burst detection. Because the densities of the latex particles and the fluid are closely matched, the particles follow the local flow well and do not settle much.

The second flow cell, shown in Fig. 1(c), is used to generate a jet flow in a 9 cm \( \times \) 9 cm square vat filled with quiescent water. The circular nozzle has an outlet 2 mm in diameter, and the tube diameter before the contraction is 5.5 mm. The nozzle is immersed in the square vat, and a small pump is used to generate a jet flow at a constant flow rate of 0.39 cm/s. The mean velocity at the nozzle exit is 12.4 cm/s, and the corresponding Reynolds number is \( Re = 248 \). This value of \( Re \) is approximately three times larger than the turbulent transition Reynolds number, \( Re_c = 80 \), for a round jet. Because of the large contraction in area (7.6:1), the bulk part of the velocity profile at the nozzle exit is flat. This uniform velocity profile vanishes quickly, and a Gaussian-like velocity profile is developed in the downstream region, 2–20 diameters away from the nozzle exit. As shown in Fig. 1(c), the direction of the momentum transfer vector \( \mathbf{q} \) (and hence the measured velocity difference) is parallel to the jet flow direction, but the separation \( L \) is at an angle of 45° to that direction.

B. Measurement of the Local Velocity

In the measurement of the velocity difference, we use two input fibers to collect the scattered light with the same \( \mathbf{q} \) (i.e., at the same scattering angle) but from two spatially separated regions in the flow. We now show that with a different optical arrangement, the fiber-optic method can also be used to measure the instantaneous local velocity \( \mathbf{v}(\mathbf{x}, t) \). Instead of collecting light from two spatially separated regions with the same \( \mathbf{q} \), we use the two input fibers to collect light from a common scattering volume in the flow but with two different momentum-transfer vec-
The collected signals at the two scattering angles are combined by a fiber-optic coupler, and the resultant light is back-scattered light from S. The frequency modulator M shifts the frequency of the light collected by input fiber 1 before it is combined via the fiber-optic coupler C with the light collected by input fiber 2. The resultant light from an output fiber of the coupler contains the beat frequency $\Delta \omega_1$ and is fed to a photodetector. Because the measured $\Delta \omega_1$ is always a positive number, one cannot tell the sign of the local velocity when zero velocity corresponds to a zero beat frequency. The frequency shift by the modulator M causes the interference fringes to move in one direction (normal to the fringes) and thus introduces an extra shift frequency to the measured beat frequency. This allows us to measure very small velocities and to determine the sign of the measured local velocity relative to the direction of the fringe motion, which is known. The other output fiber of the coupler can be used as an alignment fiber when it is connected to a small He–Ne laser. With the reversed He–Ne light coming out of the input fibers, one can directly observe the scattering volume viewed by each input fiber and align the fibers in such a way that only the scattered light from the same measuring point S is collected.

The one-beam probe has several advantages over the usual two-beam probe. To measure two orthogonal velocity components in the plane perpendicular to the incident laser beam, one only needs to add an extra pair of optical fibers and a coupler and arrange them in the plane perpendicular to that shown in Fig. 2(c); i.e., rotate the two-fiber plane shown in Fig. 2(e) by 90°. With this arrangement, the four input fibers collect the scattered light from the same scattering volume but in two orthogonal scattering planes. Because only one laser beam is needed for optical mixing, a small single-frequency diode laser, rather than a large argon–ion laser, is sufficient for the coherent light source. In addition, the one-beam arrangement does not need any optics for color and beam separations and thus can reduce the manufacturing cost considerably. With the one-beam scheme, one can make small invasive or noninvasive probes consisting of only three thin fibers. One can also make a self-contained probe containing all necessary optical fibers, couplers, and photodetectors and a single-frequency diode laser.

3. RESULTS AND DISCUSSION

A. Velocity Difference Measurements

We first discuss the measurements of the velocity difference in rigid body rotation. Figure 3(a) shows a sample oscilloscope trace of the analog output from PMT2 when the separation $L = 1.0$ mm. The signal is amplified 1250 times and bandpass-filtered with a frequency range...
of 1–10 kHz. This oscilloscope trace strongly resembles the burst signals in the standard LDV. The only difference is that the signal shown in Fig. 3(a) results from the beating of two moving particles separated by a distance \( L = 1.0 \text{ mm} \). The signal is obtained in rigid-body rotation. (b) Measured beat frequency \( \Delta \omega_2 \) as a function of separation \( L \). The circles, the oscilloscope trace; triangles, intensity correlation function \( g(\tau) \). Solid line, a linear fit to the data points.

Figure 3(b) shows the measured beat frequency \( \Delta \omega_2 \) as a function of separation \( L \). The circles are obtained from the oscilloscope trace, and the triangles are obtained from the intensity correlation function \( g(\tau) \). The two measurements agree well with each other. The solid line is the linear fit \( \Delta \omega_2 = 41.78 L \times 10^3 \text{ rad/s} \), which is in good agreement with the theoretical calculation \( \Delta \omega_2 = k_2 \omega L = 42.28 L \times 10^3 \text{ rad/s} \). This result also agrees with the previous measurements by Du et al.\(^5\). Because \( \Delta \omega_2 \) increases with \( L \), one needs to increase the laser intensity at large values of \( L \) in order to resolve \( \Delta \omega_2 \). The average photon count rate should be at least twice the measured frequency.

We now discuss the time-series measurements of \( \delta v(L, t) \) in a jet flow with use of the LDV signal processor. The jet flow has significant velocity fluctuations compared with the laminar rigid-body rotation. The measuring point is in the developing region of the jet flow, 3 diameters away from the nozzle exit, and is slightly off the centerline of the jet flow. Figure 4 shows the measured histogram \( P(\delta v) \) of the velocity difference \( \delta v(L, t) \) in the jet flow, when the separation \( L \) is fixed at \( L = 0.5 \text{ mm} \) (circles) and \( L = 0.8 \text{ mm} \) (squares), respectively. It can be seen that the measured \( P(\delta v) \) has a dominant peak and that its position changes with \( L \). Because \( \delta v(L, t) \) increases with \( L \), the peak position moves to the right for the larger value of \( L \). The solid curve in Fig. 4 is a Gaussian fit to the data points with \( L = 0.5 \text{ mm} \). The obtained mean value of \( \delta v(L, t) \) is \( \langle \delta v \rangle = 1.87 \text{ cm/s} \) and the standard deviation \( \sigma = 0.171 \text{ cm/s} \). At \( L = 0.8 \text{ mm} \), the measured \( P(\delta v) \) peaks at the value \( \langle \delta v \rangle = 2.73 \text{ cm/s} \).

In the above discussion, we have assumed that each input fiber sees only one particle at a given time and the beat signal comes from two moving particles separated by a distance \( L \). In fact, when the seeding density is high, each input fiber may see more than one particle at a given time. The scattered light from these particles can also beat and generate a self-beat frequency proportional to \( \delta v(l_0) \), where \( l_0 = 0.15 \text{ mm} \) is the laser spot size viewed by each input fiber.\(^5\) The self-beating gives rise to a small peak on the left side of the measured \( P(\delta v) \). Note that the peak position is independent of \( L \), because \( \delta v(l_0) \) is determined only by \( l_0 \), which is the same for the two measurements. It is visible from Fig. 4 that the cross-beating is dominant over the self-beating under the current experimental condition.

The intensity correlation function \( g(\tau) \) is also used to analyze the beat signal. In the experiment, we measure the histogram \( P(\delta v) \) and \( g(\tau) \) simultaneously, so that Eq. (4) can be examined in detail. Figure 5 shows the measured \( g(\tau) - 1 \) (circles) as a function of delay time \( \tau \) at \( L = 0.5 \text{ mm} \). The squares are the self-beat correlation.

![Fig. 3](image)

**Fig. 3.** (a) Oscilloscope trace of a typical beat burst between two moving particles separated by a distance \( L = 1.0 \text{ mm} \). The signal is obtained in rigid-body rotation. (b) Measured beat frequency \( \Delta \omega_2 \) as a function of separation \( L \). Circles, the oscilloscope trace; triangles, intensity correlation function \( g(\tau) \). Solid line, a linear fit to the data points.

![Fig. 4](image)

**Fig. 4.** Measured histogram \( P(\delta v) \) of the velocity difference \( \delta v(L, t) \) in the jet flow. The values of \( L \) are 0.5 mm (circles) and 0.8 mm (squares). Solid curve, Gaussian fit to the circles.
Fig. 5. Measured intensity correlation function \( g(\tau) - 1 \) as a function of delay time \( \tau \) at \( L = 0.5 \text{ mm} \) (circles). The measurements indicated by squares are obtained when one of the input fibers is blocked. The solid curve is a plot of Eq. (5).

The fitted value \( b_\gamma = 0.5 \) agrees with the expected value at \( I_1 = I_2 \). The value of \( b_\gamma \) would be 0.5 if the collected signals from the two input fibers were fully coherent and the fiber-optic coupler mixed them perfectly. The fact that the fitted value of \( b_\gamma \) is smaller than 0.5 indicates that the collected signals are not fully correlated. This is caused partially by the fact that in the present experiment the scattered light suffers relatively large number fluctuations resulting from the changing number of particles in the scattering volume. These number fluctuations produce incoherent amplitude fluctuations in the scattered light and thus introduce an extra (additive) decay to \( g(\tau) \). Because the beam-crossing time (proportional to the beam diameter) is much longer than the Doppler beat time \( 1/\Delta v \), the slow decay due to the number fluctuations can be readily identified in the measured \( g(\tau) \). This decay has an amplitude of 0.4 and has been subtracted from the measured \( g(\tau) \) shown in Fig. 5.

It is shown in Eq. (5) that in order for us to accurately measure the mean velocity difference \( \langle b \rangle \), the beat frequency \( \Delta \omega_2 = q \delta v \) must be larger than the decay rate \( \Gamma_s = q \delta v (I_0) \) for \( G_s(\tau) \) and also larger than the decay rate \( \Gamma_c = q \sigma \) resulting from the fluctuations of the velocity difference. From the measurements shown in Figs. 4 and 5, we find \( \Gamma_s = 1.33 \times 10^8 \text{ s}^{-1} \) and \( \Gamma_c = 3.8 \times 10^4 \text{ s}^{-1} \), which are indeed smaller than the beat frequency \( \Delta \omega_2 = 4.15 \times 10^7 \text{ s}^{-1} \). Because \( g(\tau) \) contains the product of \( G_s(\tau) \) and \( \exp(-q(\tau)^2/2) \) [see Eq. (5)], its decay is determined by the faster-decaying function. It can be seen from Fig. 5 that the decay of \( g(\tau) \) is controlled by \( G_s(\tau) \), which decay faster than \( \exp(-q(\tau)^2/2) \). It should be noted that in the measurements shown in Fig. 4, the beat signals are analog, and we have used a bandpass filter together with a LDV signal analyzer to resolve the beat frequency. Consequently, many low-frequency self-beat signals are filtered out. This low-frequency cutoff is apparent in Fig. 4. The measurements of \( g(\tau) \), on the other hand, are carried out in the photon counting mode, and therefore the measured \( g(\tau) \) is sensitive to all the self-beat signals as well as to the cross-beat signals. With a simple counting of particle pairs, we find that the probability of cross-beating is only twice as large as that for the self-beating.

B. Local Velocity Measurements

We now discuss the local velocity measurements, using the new optical arrangement shown in Fig. 2(a). The velocity measurements are conducted on a freely suspended flowing soap film driven by gravity. Details about the apparatus have been described elsewhere, and here we mention only some key points. A 2% solution of detergent and water is introduced at a constant rate between two long vertical nylon wires, which are held apart by small hooks. The width of the channel (i.e., the distance between the two nylon wires) is 6.2 cm over a distance of 120 cm. The measuring point is midway between the vertical wires. The soap solution is fed, through a valve, onto the apex of the channel. The film speed \( \bar{v} \), ranging from 0.5 to 3 m/s, can be adjusted with the valve. The soap film is approximately 2–6 \( \mu \text{m} \) in thickness and is seeded with micrometer-sized latex particles, which scatter light from a collimated laser beam. The light source is an argon–ion laser with a total power of 1 W. The incident laser beam is oriented perpendicular to the soap film, and the scattered light is collected in the forward direction.

To measure the rapidly changing beat frequency \( \Delta \omega_1 \), we built a fast digital correlator board for a PC. With a fast sampling rate \( f_s \), the plug-in correlator board records the time-varying intensity \( I(t) \) (number of TTL pulses from the photomultiplier tube per sample time) over a short period of time \( T \) and then calculates the (unnormalized) intensity autocorrelation function, \( A(\tau) = \langle I(t + \tau)I(t) \rangle \). Figure 6 shows an example of the measured \( A(\tau) \) as a function of delay time \( \tau \) with \( T = 30 \text{ ms} \) and \( f_s = 14.32 \text{ MHz} \). Because the burst signal \( I(t) \) is a periodic function of \( t \), the measured \( A(\tau) \) becomes an oscillatory function of \( \tau \). The frequency of the oscillation apparent in inset (a) is the beat frequency \( \Delta \omega_1 \); the amplitude of the oscillation decays at large \( \tau \). Inset (b) shows the power spectrum \( P(f) \) of the measured \( A(\tau) \); it reveals a prominent peak at 755.1 kHz. The power spectrum is obtained with a fast Fourier transform (FFT) program.

To increase the sampling rate of the velocity measurements, one needs to keep the measuring time \( T \) for each \( A(\tau) \) as short as possible. The signal-to-noise ratio for \( A(\tau) \) decreases with shorter measuring time \( T \) and with lower mean photon count rate, which was \( \sim 1 \text{ MHz} \) in the present experiment. It is found that the shortest useful
measuring time \( T_c \) is roughly 50 \( \mu s \). For this value of \( T \), \( A(\tau) \) is quite noisy, and the corresponding peak in \( P(f) \) becomes less pronounced [see Fig. 7 and inset (a)]. It is worth mentioning that if one wants to know only the periodicity of a function, rather than its actual power at different frequencies, the Scargle–Lomb method is a better alternative to the FFT. This method, which does not require evenly spaced sampling, compares the measured data with known periodic signals by using the least-square fitting procedure and determines the relevant frequencies by the goodness of the fit \( Q(f) \). It can even utilize the uneven sampling to further increase the Nyquist frequency. As shown in inset (b), the Scargle–Lomb method can still clearly identify the periodicity of the signal, even when the power spectrum \( P(f) \) [inset (a)] becomes less reliable. The total time required for measurement of the characteristic frequency is less than 1 ms.

Using the correlator board together with an average-speed PC (300 MHz), we are able to conduct accurate measurements of the local velocity with a sampling rate up to 1 kHz.

4. SUMMARY

We have developed new optical arrangements with two single-mode input fibers and a fiber-optic coupler to measure the local velocity \( \mathbf{v}(x) \) and the velocity difference, \( \delta \mathbf{v}(l) = \mathbf{v}(x + l) - \mathbf{v}(x) \), between two spatial points separated by a distance \( l \). The fibers and the coupler are polarization preserving to guarantee a high signal-to-noise ratio.

To measure the velocity difference \( \delta \mathbf{v}(l) \), the two input fibers are used to collect the scattered light with the same momentum-transfer vector \( \mathbf{q} \) but from two spatially separated regions in a flow. These regions are illuminated by a single coherent laser beam so that the collected signals interfere when combined via the fiber-optic coupler. The resultant light received by a photomultiplier tube therefore contains the beat frequency \( \Delta \omega_2 = \mathbf{q} \cdot \delta \mathbf{v}(l) \). We analyzed the beat signals using two different devices and compared the results. First, the intensity autocorrelation function \( g(\tau) \) was measured with a digital correlator. Second, a standard LDV signal processor was used to determine the instantaneous beat frequency \( \Delta \omega_2 \). With this device \( \delta \mathbf{v}(l, t) \) can be obtained in real time. The technique can be further developed to measure one component of the local-flow vorticity vector \( \mathbf{\omega}(x, t) = \nabla \times \mathbf{v}(x, t) \).

To measure the instantaneous local velocity itself, one needs only to reorient the two fibers so that they point to the same scattering volume. With this optical arrangement, we have three alternatives to measure a velocity component. They employ (i) an analog photodetector and a standard LDV signal processor (burst detector); (ii) a commercial photon correlator, such as that made by ALV; and finally (iii) a homemade digital correlator. This latter device completes a velocity measurement in less than 1 ms and is orders of magnitude cheaper than the other two alternatives. The new fiber-optic method has several advantages over the standard LDV and can be used widely in the general area of fluid dynamics. Because only one laser beam is needed to obtain two velocity components, a compact single-frequency diode laser can replace a large multifrequency argon–ion laser. By eliminating the color- and beam-separation units in the standard LDV, the one-beam scheme is less costly to implement. With more optical fiber pairs and couplers, one can carry out multipoint and multicomponent velocity measurements in various turbulent flows.

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20. For a full description of the correlator board, see http://karman.phyast.pitt.edu/horvath/corr/. The total cost for the correlator board is less than $100. The device can be duplicated for nonprofit applications without permission.
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